

LocalSolver

Solving the Capacitated Arc Routing Problem with
LocalSolver in an industrial context

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www.localsolver.com

LocalSolver

Optimization & Decision-Making Tool

> A generic, powerful solver

> 200 customers, 10,000 users, 25 countries

> Linear, non-linear and collection modeling

> Exact and heuristic techniques

> Quality solutions in seconds

Business problem

Public Asset Maintenance

Business problem : public asset maintenance

- Client's Goal: Efficient public asset maintenance.
 - Traverse entire road network within a specified area.
 - Service each road segment once.
- Constraints & Objectives:
 - Minimize total travel time and operational costs.
 - Navigate through various factors:
 - Traffic direction.
 - Speed limits.
- Desired Outcome:
 - Optimized route selection.
 - Boosted productivity and reduced overheads.



Arc routing: the underpinning concept

- Defining Arc Routing:
 - Routes are designed on arcs (or edges) rather than vertices (or nodes).
 - Ideal for problems where service is needed on roads/lanes, not at specific points.
- Ubiquity in the Industry:
 - Chinese Postman Problem (Classic example).
 - Other applications include snow removal, street cleaning, and mail delivery.
- Why It Matters:
 - CARP (Capacitated Arc Routing Problem) is NP-hard.
 - Solutions are computationally intensive and time-consuming.
 - The state-of-the-art usually involves heuristics like tabu search.
- Our Challenge:
 - Mapping the business problem to CARP.
 - Seeking optimal routes that fulfill constraints and minimize costs.



Our approach
Problem resolution

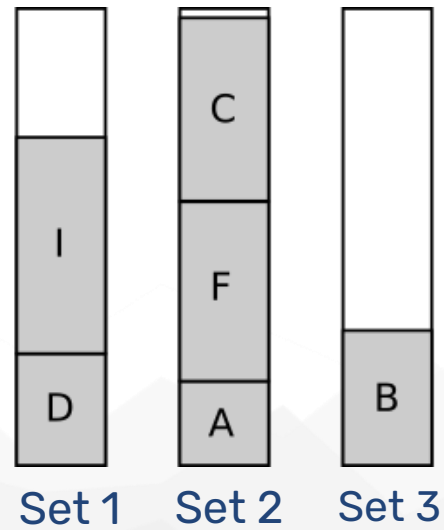
LocalSolver set modelling

Set

```
x ← set(n);
```

x : subset of {0, 1, ..., n-1}

- unicity
- Variable size

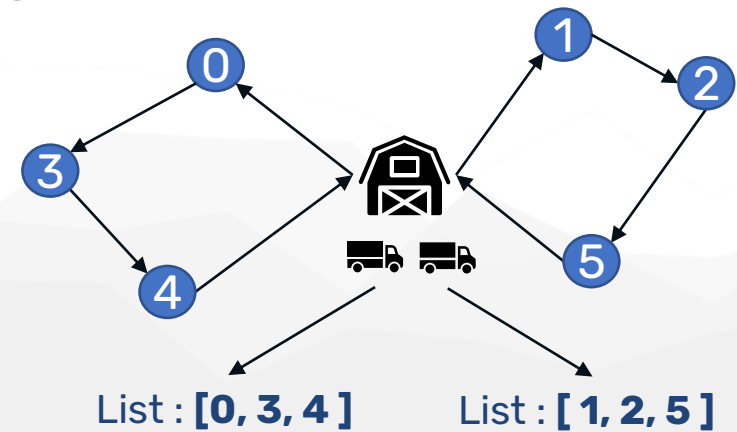


List

```
y ← list(n);
```

y : permutation of a subset of {0, 1, ..., n-1}

- unicity
- Variable size
- **order**



LocalSolver set modelling: TSP example

```
function model() {  
  // A list variable  
  cities <- list(nbCities);  
  
  // All cities must be visited  
  constraint count(cities) == nbCities;  
  
  // Minimize the total distance  
  obj <- sum(1..nbCities-1, i =>  
    distance[cities[i-1]][cities[i]]  
    + distance[cities[nbCities-1]][cities[0]]);  
  
  minimize obj;  
}
```


$$\sum_{i=1}^{n-1} \text{distance}[C_{i-1}][C_i]$$

```
PS C:\localsolver_11_0\examples\tsp> localsolver .\tsp.lsp inFileName=  
LocalSolver 11.0.20220214-Win64. All rights reserved.  
Load .\tsp.lsp...  
Run input...  
Run model...  
Run param...  
Run solver...  
  
Model: expressions = 495, decisions = 1, constraints = 1, objectives  
Param: time limit = 60 sec, no iteration limit  
  
[objective direction ]: minimize  
  
[ 0 sec, 0 itr]: No feasible solution found (infeas = 2)  
[ 1 sec, 40639 itr]: 3036  
[ 2 sec, 105606 itr]: 2835  
[ 3 sec, 161355 itr]: 2787  
[ 4 sec, 223548 itr]: 2751  
[ 5 sec, 223548 itr]: 2751  
[ 6 sec, 342635 itr]: 2725  
[ 7 sec, 342635 itr]: 2725  
[ 7 sec, 404510 itr]: 2720  
[ optimality gap ]: 0%  
  
404510 iterations performed in 7 seconds  
  
Optimal solution:  
obj = 2720  
gap = 0%  
bounds = 2720
```


LocalSolver set modelling: VRP example

Multiple trucks available:

```
tours[k] <- list(nbClients);  
constraint partition(tours);
```

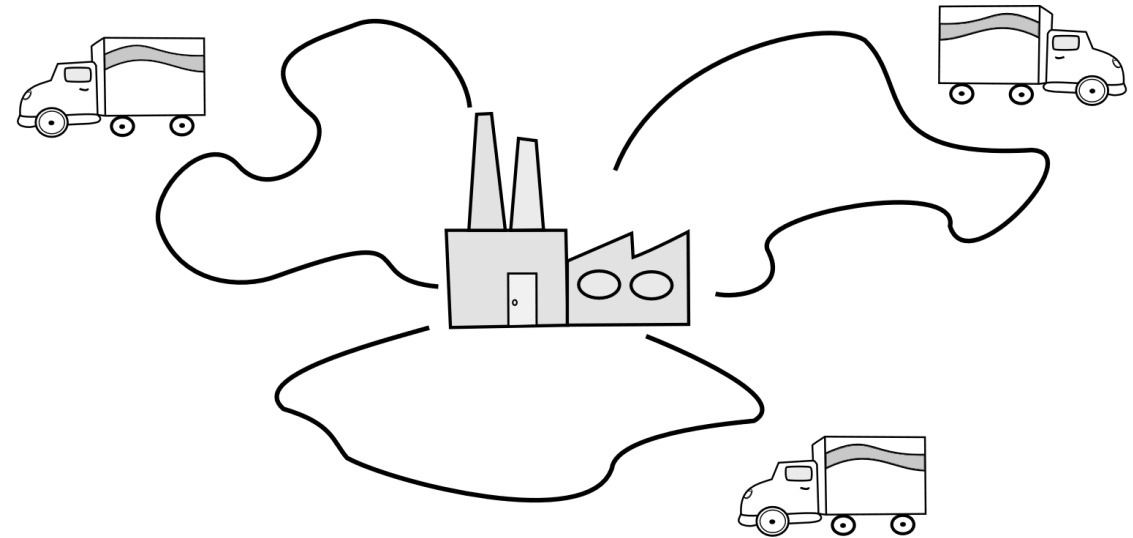
Capacity constraint for each tour k

```
sum(tours[k], c => quantity[c]) <= capa;
```



$$\sum_{c \in \text{tours}[k]} \text{quantity}[c] \leq \text{capa}$$

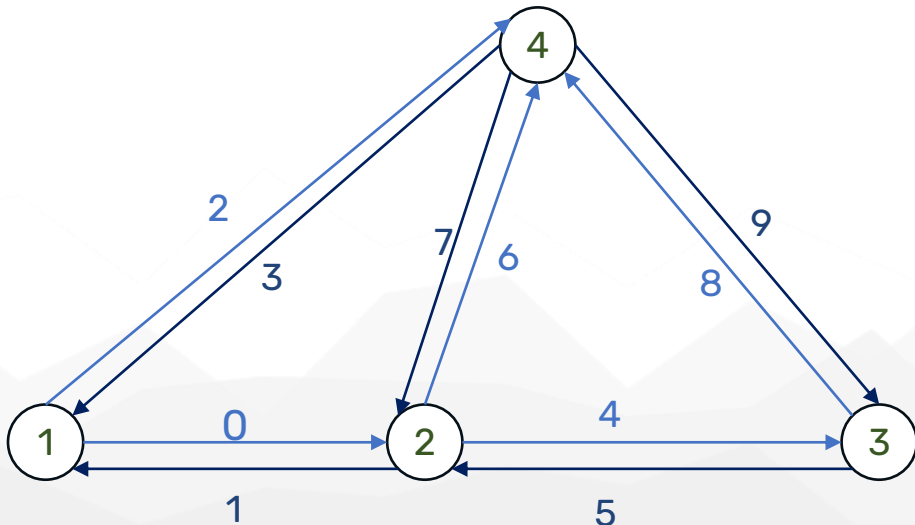
Variadic number of elements in the sum



LocalSolver set modelling: CARP

- Duplicate edges of the graph and associate a unique number
 - Only one direction of the edge can be serviced
- List variable to model vehicles

edges = [(1, 2), (2, 1), (1, 4), (4, 1), (2, 3), (3, 2), (2, 4), (4, 2), (3, 4), (4, 3)]



edges = [0, 1, 2, 3, 4, 5, 6, 7, 8, 9]

Duplicate values are **alternatives**

LSP model overview

```
// Sequence of edges visited and "serviced" by each truck
// A sequence can contain an edge in one direction or its reverse
edgesSequences[k in 0..nbTrucks-1] <- list(2 * nbRequiredEdges);

// An edge must be serviced by at most one truck
constraint disjoint(edgesSequences);

// An edge can be travelled in both directions, but its demand must be satisfied only once
for [i in 0..nbRequiredEdges-1] {
    constraint contains(edgesSequences, 2 * i) + contains(edgesSequences, 2 * i + 1) == 1;
}
```

LSP model overview

```
for [k in 0..nbTrucks-1] {  
  local sequence <- edgesSequences[k];  
  local c <- count(sequence);  
  
  // Quantity in each truck  
  routeQuantity <- sum(0..c-1, i => requiredEdgesDemands[sequence[i]]);  
  
  // Capacity constraint : a truck must not exceed its capacity  
  constraint routeQuantity <= truckCapacity;  
  
  // Distance travelled by each truck  
  routeDistance[k] <- sum(1..c-1, i => requiredEdgesCosts[sequence[i]]  
    + distanceBetweenEdges[sequence[i - 1]][sequence[i]])  
    + (c > 0 ? requiredEdgesCosts[sequence[0]] + distanceFromDepot[sequence[0]]  
    + distanceToDepot[sequence[c - 1]] : 0);  
}
```

LSP model overview

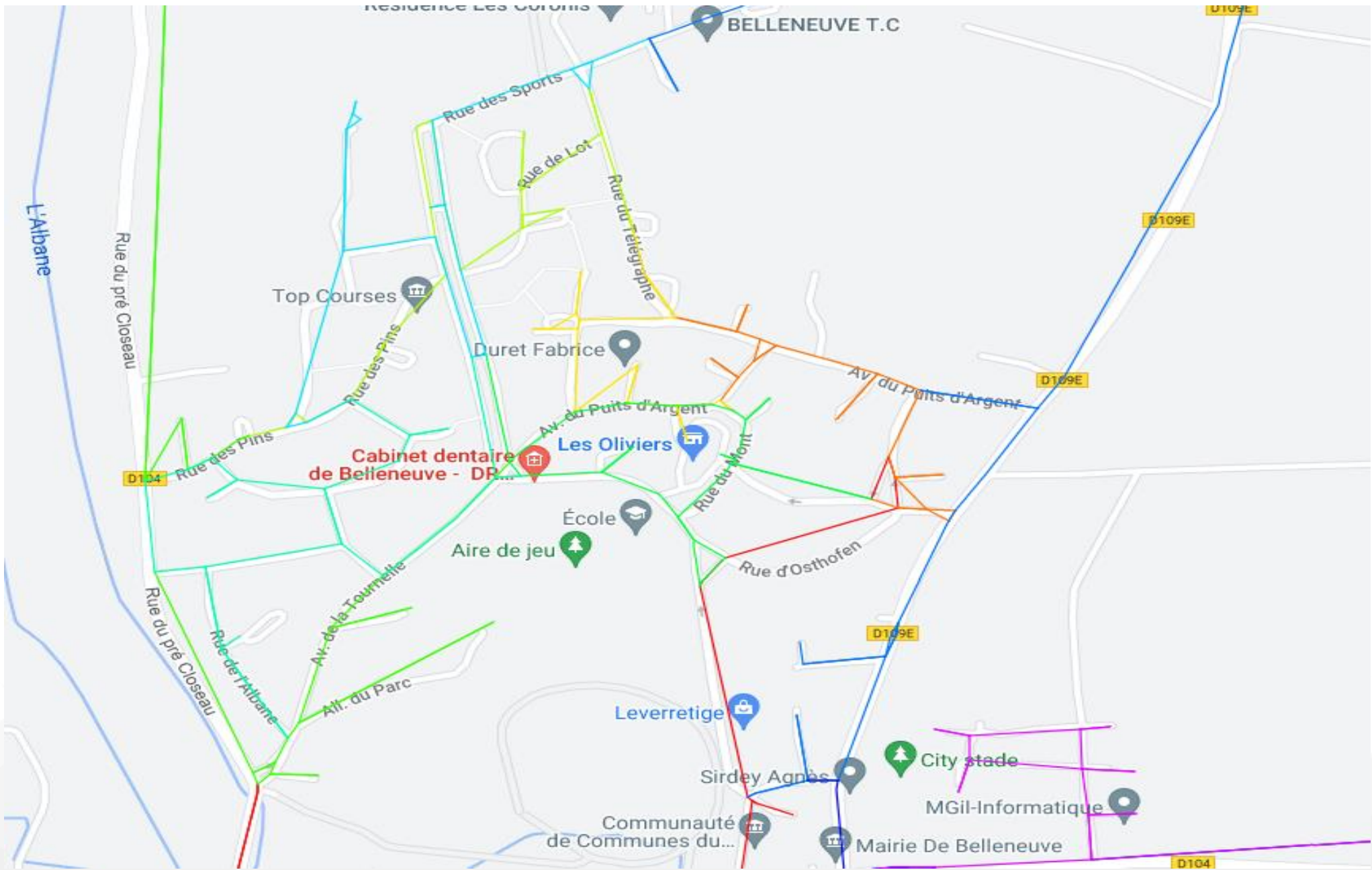
```
// Total distance travelled
```

```
totalDistance <- sum[k in 0..nbTrucks-1](routeDistance[k]);
```

```
// Objective: minimize the distance travelled
```

```
minimize totalDistance;
```

Results obtained



Numeric results

- J. Brandão, et R. Eglese. A Deterministic Tabu Search Algorithm for the Capacitated Arc Routing Problem (CARP), Computers & Operations Research., 2008
- 34 instances of 3 categories
 - 98 edges
 - 190 edges
 - 375 edges

Results

Instance	Gap to BK in 60 sec	Gap to BK in 600 sec
98	0.27%	-0.19%
egl-e1-A	0.00%	0.00%
egl-e1-B	0.60%	0.00%
egl-e1-C	0.32%	0.00%
egl-e2-A	0.00%	0.00%
egl-e2-B	0.11%	-0.36%
egl-e2-C	0.55%	-0.71%
egl-e3-A	0.00%	0.00%
egl-e3-B	0.18%	-0.22%
egl-e3-C	-0.33%	-0.58%
egl-e4-A	0.05%	0.05%
egl-e4-B	0.81%	0.18%
egl-e4-C	0.93%	-0.65%

Results

Instance	Moyenne de Gap to BK en 60 sec	Moyenne de Gap to BK en 600 sec
⊕ 98	0.27%	-0.19%
⊖ 190	1.25%	0.03%
egl-s1-A	0.00%	0.00%
egl-s1-B	-0.73%	-0.73%
egl-s1-C	0.76%	0.00%
egl-s2-A	2.29%	0.07%
egl-s2-B	4.86%	2.85%
egl-s2-C	0.18%	-1.09%
egl-s3-A	0.83%	0.09%
egl-s3-B	-0.52%	-1.43%
egl-s3-C	1.76%	0.31%
egl-s4-A	1.01%	-0.44%
egl-s4-B	-0.33%	-0.93%
egl-s4-C	4.89%	1.68%

Results

Instance	Moyenne de Gap to BK en 60 sec	Moyenne de Gap to BK en 600 sec
+ 98	0.27%	-0.19%
+ 190	1.25%	0.03%
- 375	0.32%	-0.45%
egl-g1-A	-0.30%	-0.81%
egl-g1-B	1.84%	0.84%
egl-g1-C	-0.01%	-0.38%
egl-g1-D	0.94%	0.28%
egl-g1-E	2.33%	0.94%
egl-g2-A	0.54%	-0.54%
egl-g2-B	-0.46%	-1.01%
egl-g2-C	-2.32%	-2.63%
egl-g2-D	0.18%	-0.84%
egl-g2-E	0.50%	-0.34%

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